

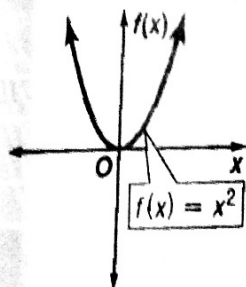
as  $x$  approaches positive infinity.

## Concept Summary

## End Behavior of a Polynomial Function

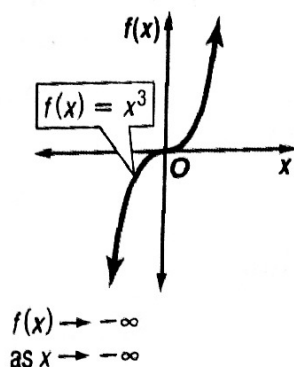
**Degree:** even  
**Leading Coefficient:** positive  
**End Behavior:**

$$\begin{array}{ll} f(x) \rightarrow +\infty & f(x) \rightarrow +\infty \\ \text{as } x \rightarrow -\infty & \text{as } x \rightarrow +\infty \end{array}$$



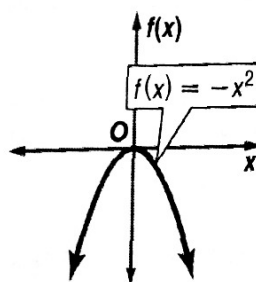
**Degree:** odd  
**Leading Coefficient:** positive  
**End Behavior:**

$$\begin{array}{l} f(x) \rightarrow +\infty \\ \text{as } x \rightarrow +\infty \end{array}$$



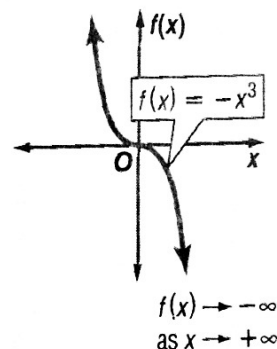
**Degree:** even  
**Leading Coefficient:** negative  
**End Behavior:**

$$\begin{array}{ll} f(x) \rightarrow -\infty & f(x) \rightarrow -\infty \\ \text{as } x \rightarrow -\infty & \text{as } x \rightarrow +\infty \end{array}$$



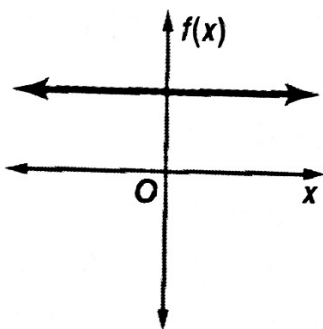
**Degree:** odd  
**Leading Coefficient:** negative  
**End Behavior:**

$$\begin{array}{l} f(x) \rightarrow +\infty \\ \text{as } x \rightarrow -\infty \end{array}$$

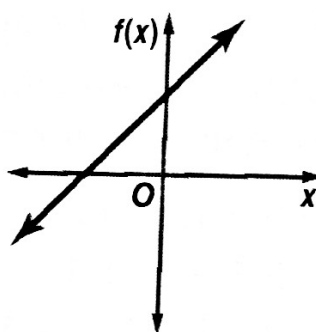


**GRAPHS OF POLYNOMIAL FUNCTIONS** The general shapes of the graphs of several polynomial functions are shown below. These graphs show the *maximum* number of times the graph of each type of polynomial may intersect the  $x$ -axis. Recall that the  $x$ -coordinate of the point at which the graph intersects the  $x$ -axis is called a *zero* of a function. How does the degree compare to the maximum number of real zeros?

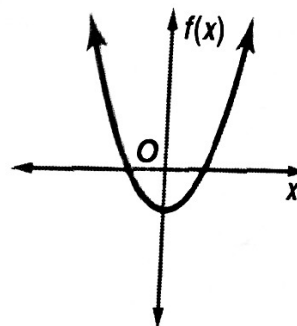
Constant function  
Degree 0



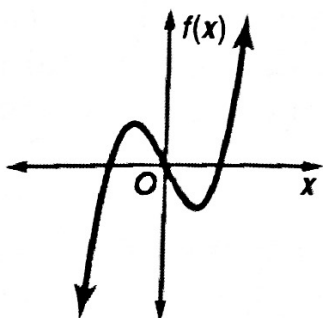
Linear function  
Degree 1



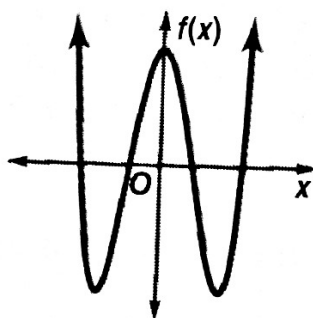
Quadratic function  
Degree 2



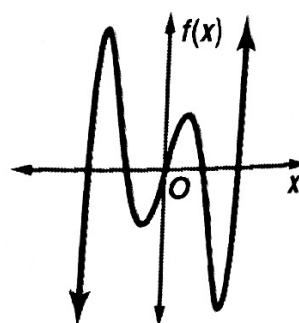
Cubic function  
Degree 3



Quartic function  
Degree 4



Quintic function  
Degree 5



Notice the shapes of the graphs for even-degree polynomial functions and odd-degree polynomial functions. The degree and leading coefficient of a polynomial function determine the graph's end behavior.